Markov Sick-Sicker model

with age dependency

The DARTH workgroup

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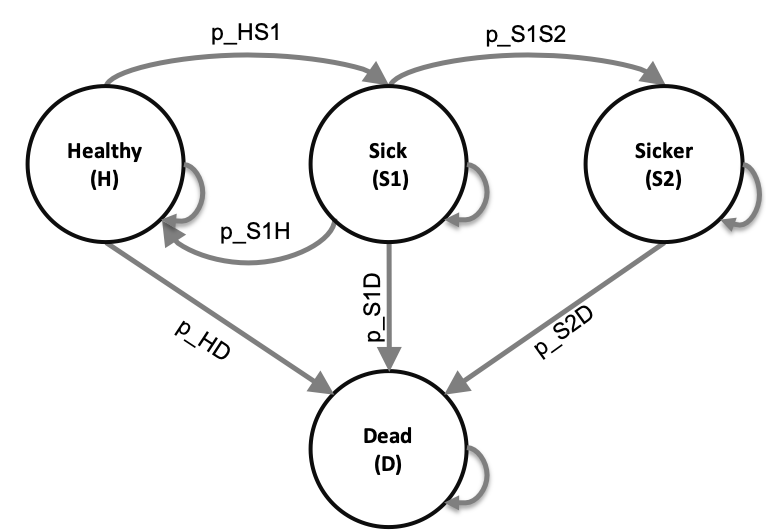
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# Exercise I: Construct a Markov Model of the Sick-Sicker Disease

In this exercise, we will model a hypothetical disease that affects individuals with an average age of 25 years and results in increased mortality, increased healthcare costs, and reduced quality of life. The disease has two levels; affected individuals initially become sick but can subsequently progress and become sicker. Two alternative strategies exist for this hypothetical disease: a no-treatment and a treatment strategy. Under the treatment strategy, individuals in the sick and sicker states are treated until they recover (only if sick; individuals in the sicker state cannot recover) or die. The cost of the treatment is additive to the baseline healthcare costs of being sick or sicker. The treatment improves quality of life for those individuals who are sick but has no impact on the quality of life of those who are sicker. Unfortunately, it is not possible to reliably differentiate between people in the sick and sicker states, so treatment cannot be targeted to only those in the sick state. You are asked to evaluate the cost-effectiveness of the treatment.

To model this disease, we will rely on a state-transition cohort model, called the Sick-Sicker model, first described by Enns et al. The Sick-Sicker model consists of four health states: Healthy (H), two disease states, Sick (S1) and Sicker (S2), and Dead (D) (Figure 1). All individuals start in the Healthy state. Over time, healthy individuals may develop the disease and can progress to S1. Individuals in S1 can recover (return to state H), progress further to S2 or die. Individuals in S2 cannot recover (i.e. cannot transition to either S1 or H). Individuals in H have a baseline probability of death; individuals in S1 and S2 experience increased mortality compared to those in the H state, given in terms of hazard ratios. These ratios are used to calculate the probabilities of dying when in S1 and S2.



Schematic representation of the Sick-Sicker model

## Tasks

Using the template markov\_sick-sicker\_template.Rmd, please do the following.

1. Build the Markov model in R for the no-treatment and treatment strategies including age-dependent mortality.
2. Plot the survival curve for the cohort under no-treatment.
3. Estimate the cost-effectiveness of treatment vs no-treatment.
4. Create a cost-effectiveness table with all results of interest.

**Table I: Input parameters**

|  |  |  |
| --- | --- | --- |
| **Parameter** | **R name** | **Value** |
| Time horizon | n\_t | 30 years |
| Cycle length |  | 1 year |
| Names of health states | v\_n | H, S1, S2, D |
| Annual discount rate (costs/QALYs) | d\_r | 3% |
| Annual transition probabilities conditional on surviving |  |  |
| - Disease onset (H to S1) | p\_HS1 | 0.15 |
| - Recovery (S1 to H) | p\_S1H | 0.5 |
| - Disease progression (S1 to S2) | p\_S1S2 | 0.105 |
| Annual mortality |  |  |
| - All-cause mortality (H to D) | p\_HD | HMD - info below |
| - Hazard ratio of death in S1 vs H | hr\_S1 | 3 |
| - Hazard ratio of death in S2 vs H | hr\_S2 | 10 |
| Annual costs |  |  |
| - Healthy individuals | c\_H | $2,000 |
| - Sick individuals in S1 | c\_S1 | $4,000 |
| - Sick individuals in S2 | c\_S2 | $15,000 |
| - Dead individuals | c\_D | $0 |
| - Additional costs of sick individuals treated in S1 or S2 | c\_trt | $12,000 |
| Utility weights |  |  |
| - Healthy individuals | u\_H | 1.00 |
| - Sick individuals in S1 | u\_S1 | 0.75 |
| - Sick individuals in S2 | u\_S2 | 0.50 |
| - Dead individuals | u\_D | 0.00 |
| Intervention effect |  |  |
| - Utility for treated individuals in S1 | u\_trt | 0.95 |

\*Note: To calculate the probability of dying from S1 and S2, use the hazard ratios provided. To do so, first convert the probability of dying from healthy, p\_HD, to a rate; then multiply this rate by the appropriate hazard ratio; finally, convert this rate back to a probability. Recall that you can convert between rates and probabilities using the following formulas: and . The package darthtools also has the functions prob\_to\_rate and rate\_to\_prob that might be of use to you.

* 1. *HMD* : This is the Human mortality database. We provide you a files called HMD\_USA\_Mx\_2015.csv with the age specific mortality rates. The data has the columns X, Year, Age, Female, Male, Total and OpenInterval. We will use the overal age specific mortality rate from the Total column.

## Age specific all cause mortality

The code below shows you how to get the data into your R environment. We also provide this in the template

## X Year Age Female Male Total OpenInterval  
## 1 9103 2015 0 0.005386 0.006404 0.005907 FALSE  
## 2 9104 2015 1 0.000350 0.000452 0.000402 FALSE  
## 3 9105 2015 2 0.000228 0.000277 0.000253 FALSE  
## 4 9106 2015 3 0.000163 0.000228 0.000196 FALSE  
## 5 9107 2015 4 0.000127 0.000167 0.000147 FALSE  
## 6 9108 2015 5 0.000113 0.000157 0.000136 FALSE

# Transition probabilities (per cycle) and hazard ratios  
# Read age-specific mortality rates from csv file  
# if you have the data in the same folder as you markdown  
#lt\_usa\_2005 <- read.csv("HMD\_USA\_Mx\_2015.csv")  
  
# if you have a data folder  
lt\_usa\_2005 <- read.csv("../data/HMD\_USA\_Mx\_2015.csv")  
  
v\_r\_HD <- lt\_usa\_2005 %>%   
 filter(Age >= age & Age <= (max\_age-1)) %>%  
 select(Total) %>%  
 as.matrix()